

8-A

### Growth: Linear versus Exponential

- **Linear Growth** occurs when a quantity grows by some fixed *absolute* amount in each unit of time.
- **Exponential Growth** occurs when a quantity grows by the same fixed *relative* amount—that is, by the same percentage—in each unit of time.

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### Key Facts about Exponential Growth

- **Exponential growth** leads to repeated doublings. With each doubling, the amount of increase is approximately equal to the sum of all preceding doublings.
- **Exponential growth** cannot continue indefinitely. After only a relatively small number of doublings, exponentially growing quantities reach impossible proportions.

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### Rule of 70 Approximations

- **Doubling Time**  
For a quantity growing exponentially at a rate of P% per time period, the doubling time is approximately
 
$$T_{\text{double}} \approx \frac{70}{P}$$
- **Half-Life Period**  
For a quantity growing exponentially at a rate of P% per time period, the doubling time is approximately
 
$$T_{\text{half-life}} \approx \frac{70}{P}$$

*For both doubling and halving, this approximation works best for small growth rates and breaks down for growth rates over about 15%*

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### Exponential Growth vs. Decay

**Exponential Growth**

$\text{new value} = \text{initial value} \times 2^{t/T_{\text{double}}}$

**Exponential Decay**

$\text{new value} = \text{initial value} \times \left(\frac{1}{2}\right)^{t/T_{\text{half-life}}}$

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### Exact Doubling Time and Half-Life Formulas

$$T_{\text{double}} = \frac{\log 2}{\log(1+r)}$$

Exponential Growth  
(given that  $r > 0$ )

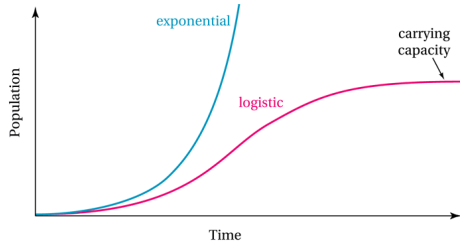
$$T_{\text{half}} = \frac{-\log 2}{\log(1+r)} \text{ or } \frac{\log(1/2)}{\log(1+r)}$$

Exponential Decay  
(given that  $r < 0$ )

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## Exponential versus Logistic Growth

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## Overall Growth Rate and Logistic Growth Rate

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### Overall Growth

The world population growth rate is the difference between the birth rate and the death rate:

$$\text{growth rate} = \text{birth rate} - \text{death rate}$$

### Logistic Growth

The logistic growth rate is dependent upon the ratio of current population to carrying capacity:

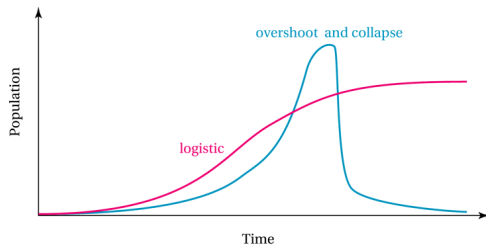
$$\text{growth rate} = \text{base rate} \times (1 - \text{population} / \text{carrying capacity})$$

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## Overshoot and Collapse

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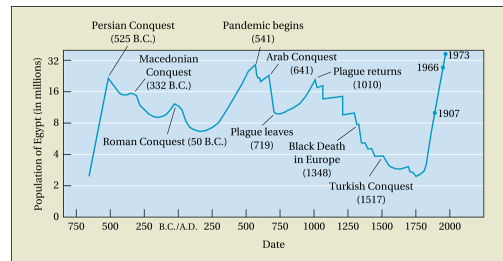


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## Difficulties of Population Prediction

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The historical population of Egypt

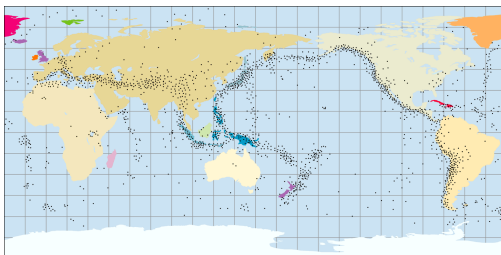
SOURCE: T.H. Hollingsworth, *Historical Demography* (Ithaca, NY: Cornell University Press, 1969).

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## Distribution of Earthquakes

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The distribution of earthquakes around the world.  
Each dot represents an earthquake.  
SOURCE: U.S. Geological Survey

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## Measuring Sound

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- The **decibel scale** is used to compare the loudness of sounds.
- The loudness of a sound in decibels is defined by the following equivalent formulas:

$$\text{loudness in dB} = 10 \log_{10} \left( \frac{\text{intensity of the sound}}{\text{intensity of the softest audible count}} \right)$$

or

$$\frac{\text{intensity of the sound}}{\text{intensity of the softest audible sound}} = 10^{\frac{\text{loudness in dB}}{10}}$$

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## Typical Sounds in Decibels

**TABLE 8.5** Typical Sounds in Decibels

DECIBELS	TIMES LOUDER THAN	
	SOFTTEST AUDIBLE SOUND	EXAMPLE
140	$10^{14}$	jet at 30 meters
120	$10^{12}$	strong risk of damage to human ear
100	$10^{10}$	siren at 30 meters
90	$10^9$	threshold of pain for human ear
80	$10^8$	busy street traffic
60	$10^6$	ordinary conversation
40	$10^4$	background noise in average home
20	$10^2$	whisper
10	$10^1$	rustle of leaves
0	1	threshold of human hearing
-10	0.1	inaudible sound

## pH Scale

- The pH scale is defined by the following equivalent formula:

$$\text{pH} = -\log_{10}[\text{H}^+] \quad \text{or} \quad [\text{H}^+] = 10^{-\text{pH}}$$

- where  $[\text{H}^+]$  is the hydrogen ion concentration in moles per liter. Pure water is neutral and has a pH of 7. Acids have a pH lower than 7 and bases have a pH higher than 7.